

# Deep Multi-task Learning with Cross Connected Layer for Slot Filling

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**Abstract.** Slot filling is a critical subtask of Spoken language understanding (SLU) in task-oriented dialogue systems. This is a common scenario that different slot filling tasks from different but similar domains have overlapped sets of slots (shared slots). In this paper, we propose an effective deep multi-task learning with Cross Connected Layer (CCL) to capture this information. The experiments show that our proposed model outperforms some mainstream baselines on the Chinese E-commerce datasets. The significant improvement in the F1 score of the shared slots proves that CCL can capture more information about shared slots.

**Keywords:** Multi-task learning · Slot filling · Shared slots · CCL

## 1 Introduction

Spoken Language Understanding, which aims to interpret the semantic meanings conveyed by input utterances, is an important component in task-oriented dialog systems. Slot filling, a sub-problem of SLU, extracts semantic constituents by using the words of input utterance to fill in predefined slots in a semantic frame [1].

Slot filling problem can be regarded as a sequence labeling task, which assigns an appropriate semantic label to each word with a given input utterance. State-of-the-art sequence labeling models are typically based on BiLSTM-CRF [2, 3]. There are a variety of task-oriented dialog systems of different domains such as air travel [4], computer shopping guide and phone shopping guide.

It is common that there is semantic correspondence between slots defined in different domains. Consider these two sentences:

1. I want to buy a computer which is about  $\{price\_middle \text{ four thousand yuan}\}$  and has a ram of  $\{ram\_size \text{ 8 G}\}$ .
2. I plan to get a new mobile phone of  $\{brand \text{ Huawei}\}$ , which costs about  $\{price\_middle \text{ 3000 yuan}\}$ .

These two sentences respectively come from the domain of computer shopping guide and the domain of phone shopping guide. We can find out that these two sentences have the same slot “price\\_middle” which means the median of

psychological price. We denote the same slot between the slot filling tasks of different domains as shared slot.

Multi-task Learning (MTL) has been applied to various models and problems. But most of the current multitasking learning methods [5] only share parameters at the bottom layer. We believe that this model structure can't make good use of the information of shared slots. To achieve this goal, we propose the CCL to encourage all tasks to learn a common label representation. We combine the multi-task BiLSTM-CRF model and this layer to address for slot filling problem with shared slots.

The main contribution of this work lies on:

1. We propose an original MTL architecture with CCL to capture the information of shared slots. The experiment results show the effectiveness of the CCL.
2. We build three datasets for slot filling tasks on three domains: computer, mobile phone, and camera. These datasets enrich the experimental data in Chinese slot filling field.

The rest of the paper is organized as follows: Section 2 introduces related work. Section 3 describes the details of our method. In Section 4, we illustrate our experiments. Finally, we draw our conclusions in Section 5.

## 2 Related Work

Our work is in line with existing methods using neural network for slot filling. Slot filling can be treated as a sequence labeling problem. Here, we use the IOB [6] scheme for representing segmentation. In recent years, deep learning approaches have been explored due to its successful application in many NLP tasks. For slot filling problem, deep learning search has started as extensions of DNNs and DBNs [7] and is sometimes merged with CRFs [8]. Especially with the rediscovery of LSTM cells [9] for RNNs, this architecture has started to emerge [10]. Many neural network architectures have been used such as simple RNNs [11, 12], convolutional neural networks (CNNs) [13], LSTMs [14] and variations like encoder-decoder [15] and external memory [16]. In general, these works adopt a BiLSTM as the major labeling architecture to extract various features, then use a CRF layer [2] to model the label dependency.

MTL has attracted increasing attention in both academia and industry recently. By jointly learning across multiple tasks [17], we can improve performance on each task and reduce the need for labeled data. There has been several attempts of using multi-task learning on sequence labeling task [18–21]. Hakkani-Tur et al. [5] proposed a multi-domain SLU model using BiLSTM. They train the multi-domain model by using data from all the domains and let the data from each domain to reinforce each other. Kim et al. proposed neural generalization of the feature augmentation domain adaptation methods [22]. Their model uses an LSTM to captures global patterns by training on data.

### 3 Model

To better utilize the shared slots' information between multiple tasks, we propose a novel multi-task architecture with CCL (MT-BiLSTM-CRF-CCL). As shown in Fig.1, the architecture contains four layers: (1) Embedding Layer, (2) Shared BiLSTM Layer, (3) Cross Connected Layer, (4) Task-oriented CRF Output Layer.

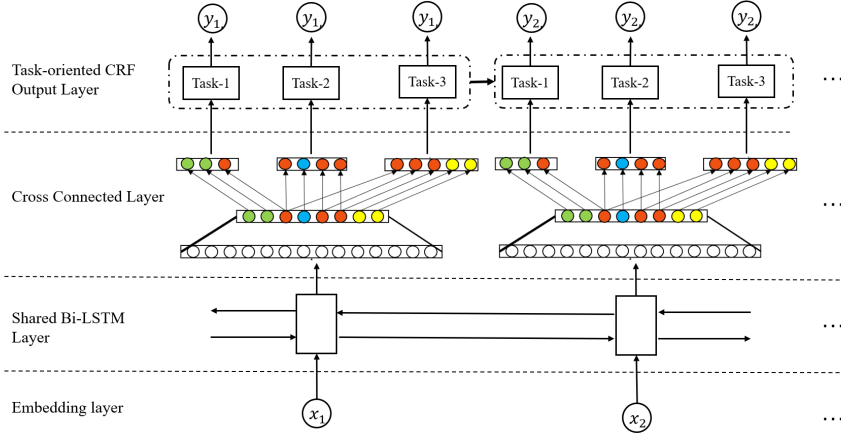


Fig. 1: The architecture of our proposed model

When learning multiple task  $t = \{1, 2, \dots, T\}$ , we denote the task-specific label set as  $L_t$ . Each task shares the same BiLSTM layer to get the representations, partially share the last fully connected layer, and has their own CRF output layer. In the training procedure, each task updates the whole model's parameters one by one in each training epoch. Different from previous multi-task work, we propose a novel CCL for multi-task learning to capture the information of shared slots. We will introduce the details of these four layers as follows.

#### 3.1 Embedding Layer

In this layer, we take the characters as the input of our model. It has been shown that character-based methods outperform word-based methods for Chinese sequence tagging problem [23, 24]. In the character sentence  $S = \{c_1, c_2, \dots, c_n\}$ , each character  $c_i$  is represented using

$$x_i^c = e^c(c_i) \quad (1)$$

where  $e^c$  denotes a character embedding looking table.

### 3.2 Shared BiLSTM Layer

Long short-term memory (LSTM) [9] is a recurrent neural network (RNN) that models interactions between input vectors and hidden layers. Since most sequence tagging tasks benefit from both historical and future context information of the words when deciding on the label for a given token, most LSTM sequence taggers use the bi-directional model. The BiLSTM uses two LSTMs to enable the hidden states to capture both historical and future context information of the words.

We build a shared BiLSTM layer for several tasks to get the representation of the input sentences. The shared BiLSTM layer is trained with the feedback by all the tasks. Mathematically, the input of this BiLSTM layer is the output of the embedding layer  $X = \{x_1^c, x_2^c, \dots, x_n^c\}$ . The output of BiLSTM layer is a sequence of the hidden states for each input word, denoted as  $H = (h_1, h_2, \dots, h_n)$ . Each final hidden state is the concatenation of the forward  $\vec{h}$  and backward  $\overleftarrow{h}$  hidden states. We view BiLSTM as a function  $BiLSTM(x_i)$ :

$$\vec{h}_i = LSTM(x_i, \vec{h}_{i-1}), \overleftarrow{h}_i = LSTM(x_i, \overleftarrow{h}_{i-1}) \quad (2)$$

$$BiLSTM(x_i) = h_i = \vec{h}_i(x_i) \oplus \overleftarrow{h}_i(x_i) \quad (3)$$

In addition, we stack multiple BiLSTMs to make the model deeper, in which the output  $h_i^l$  of layer  $l$  becomes the input of layer  $l+1$ , e.g.  $h_i^{l+1} = BiLSTM^{l+1}(h_i^l)$ .

### 3.3 Cross Connected Layer

In previous multi-task work on multi-domain, each task makes a task-oriented fully connected layer or a task-oriented CRF as the output layer. The information between multiple tasks is shared at the BiLSTM layer. But this multi-task model only shares parameters at the bottom layer, it is difficult for multi-task model to obtain information between slot labels. Therefore, in order to better extract the information of shared slots, we propose a novel CCL to encourage the multi-task model to learn a shared label representation between different tasks. CCL has two processes: union process and separate process.

**Union process:** this process transforms the hidden states  $h_i$  into the union label representation  $D_i$  on the union slots  $L_u$ .

The union slots  $L_u$  is

$$L_u = \bigcup_t L_t. \quad (4)$$

The shared label representation  $D_i$  is

$$D_i = h_i W_{fc}. \quad (5)$$

Here, the dimensionality of  $W_{fc}$  is  $s \times l$  where  $s$  is the hidden size and  $l$  is the size of union slots  $L_u$ .

The parameters will be updated by all of shared slots' training data of all tasks, and this make our model get better use of the information of shared slots.

**Separate process:** this process convert the shared label representation  $D_i$  to the task-oriented label representation  $D_{(i,t)}$  for task  $t$ . For each task-oriented label representation  $D_{(i,t)}$ , it only use the label representation of corresponding slots. This process avoids the problem caused by that we mix all slots into one label representation. The procedure of the separate algorithm is summarized as Algorithm 1.

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**Algorithm 1:** Separate slots

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for  $t$  in  $1, 2, \dots, T$  do
  for  $(index, slot)$  in  $L_u$  do
    if  $slot$  in  $L_t$  then
       $D_{(i,t)}$ .append( $D_i[index]$ )
    end
  end
end

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Among the algorithm, the “index” and “slot” here represent the subscript and label value of the  $L_u$  respectively.

### 3.4 Task-oriented CRF Output Layer

Label dependencies are crucial for sequence labeling tasks. For example, in the task with IOB annotation, it is not only meaningless but illegal to annotate I-price\_middle after B-brand (i.e., mixing the price and the brand). Therefore, jointly decoding a chain of labels can ensure the resulting label sequence to be meaningful. CRF has been included in most state-of-the-art models to capture such information and further avoid generating illegal annotations [25]. Consequently, we build a task-oriented standard CRF layer upon the CCL layer for all tasks.

The CRF layer takes the output of the CCL  $D_{(1,t)}, D_{(2,t)}, \dots, D_{(n,t)}$  as input. For task  $t$ , the probability of a label sequence  $y_t = l_1, l_2, \dots, l_n$  is

$$P(y_t|s) = \frac{\exp(\sum_i (W_{CRF-t}^{l_i} h_{(i,t)} + b_{CRF-t}^{(l_{(i-1,t)}, l_{(i,t)})}))}{\sum_{y'} (\exp(\sum_i (W_{CRF-t}^{l_i} h_{(i,t)} + b_{CRF-t}^{(l_{(i-1,t)}, l_{(i,t)})})))} \quad (6)$$

where  $y'$  represents an arbitrary label sequence,  $W_{CRF-t}^{l_i}$  is a model parameter specific to  $l_i$  of task  $t$ , and  $b_{CRF-t}^{(l_{(i-1,t)}, l_{(i,t)})}$  is a bias specific to  $l_{(i-1,t)}$  and  $l_{(i,t)}$ .

We predict the output sequence by using the Viterbi algorithm [26] to find the highest scored label sentence. Given a set of training data  $\{(s_i, y_i)_{i=1}^N\}$ , the

loss function is

$$L = - \sum_{l=1}^N \log(P(y_l | s_l)). \quad (7)$$

## 4 Experiments

### 4.1 Datasets

We evaluate the proposed model on the datasets across multiple domains: E-commerce Computer, E-commerce Camera, E-commerce Phone. These datasets are obtained from the websites of the camera, computer and mobile phone. Then, we manually filter and tag the data to get the final datasets. These datasets are divided into three parts: train set, development set and test set. The vocabulary size of the dataset is 1189. The Table.1 shows the statistics of these datasets. These datasets are available online<sup>3</sup>.

Table 1: The statistics of the datasets

Dataset	Train	Dev	Test	Label num	Avg. length
E-commerce Computer	6145	1087	1113	47	17.20
E-commerce Camera	3408	522	521	25	21.84
E-commerce Phone	3455	626	616	37	19.00

### 4.2 Experimental Setting

We use the 100-dimensional character embedding from Wikimedia documents trained by word2vec. For the shared BiLSTM Layer, we use a 2-layers BiLSTM. The hidden size of BiLSTM is set to be 100. The training procedure consists of two stages: joint training and fine-tuning. We use the Adam optimizer to train our architecture. The batch size 2 and 32 are applied in joint training stage and fine-tuning stage, respectively. The dropout rate is set to be 0.25.

In this experiment, we use several mainstream models including BiLSTM, BiLSTM-CRF, MT-BiLSTM, MT-BiLSTM-CRF. For the single task, we use a BiLSTM and a fully connected layer to form BiLSTM model and apply a CRF layer upon the BiLSTM layer to get BiLSTM-CRF model. For multi-task model (MT-BiLSTM, MT-BiLSTM-CRF), we share the embedding layer and the first LSTM layer.

<sup>3</sup> <https://github.com/JansonKong/Deep-Multi-task-Learning-with-Cross-Connected-Layer-for-Slot-Filling>

### 4.3 Experimental Results

We compare the performance of our models to all four baselines. The comparison is conducted on three datasets: E-commerce camera dataset, E-commerce computer dataset, E-commerce phone dataset. The evaluation measures are widely-used Precision, Recall and F1-Measure in information retrieval area. The results are shown on Table.2.

Table 2: Experiment results on three datasets

Model	camera			computer			phone		
	P	R	F1	P	R	F1	P	R	F1
BiLSTM	0.878	0.904	0.8908	0.837	0.823	0.8295	0.812	0.797	0.8045
BiLSTM-CRF	0.904	0.910	0.9071	0.896	0.864	0.8800	0.863	0.863	0.8677
MT-BiLSTM	0.909	0.910	0.9092	0.870	0.837	0.8534	0.892	0.902	0.8969
MT-BiLSTM-CRF	0.916	0.919	0.9175	0.905	0.891	0.8981	0.907	0.910	0.9086
<b>MT-BiLSTM-CCL</b>	0.944	<b>0.952</b>	0.9480	0.908	0.908	0.9078	0.893	0.914	0.9033
<b>MT-BiLSTM-CRF-CCL</b>	<b>0.957</b>	0.951	<b>0.9541</b>	<b>0.931</b>	<b>0.924</b>	<b>0.9274</b>	<b>0.916</b>	<b>0.926</b>	<b>0.9207</b>

From the results, on the the E-commerce camera dataset, single-task BiLSTM model obtains a F1-score of 89.08% and the single-task BiLSTM-CRF model obtains a F1-score of 90.71%. Compared with single-task models, the multi-task models (MT-BiLSTM, MT-BiLSTM-CRF, MT-BiLSTM-CCL, MT-BiLSTM-CRF-CCL) get better results which prove that multi-task models work better on these tasks. The results present that our MT-BiLSTM-CRF-CCL model outperform all the neural network baselines (p-value<0.005). Compared with the strong baseline MT-BiLSTM-CRF model (p-value<0.005), MT-BiLSTM-CRF-CCL model increases respectively by 3.66%, 2.93% and 1.21% in the F1 scores on these datasets.

In order to verify the effectiveness of CCL, We also combine MT-BiLSTM model with CCL to get MT-BiLSTM-CCL model. The results show that the MT-BiLSTM-CCL model has made a huge improvement in the F1 score compared with MT-BiLSTM model. This result proves the effectiveness of the CCL.

To verify that CCL layer can effectively utilize the information of shared slots, we calculate the F1 values of shared slots and non-shared slot respectively. The results are showed on Fig 2. Compared with the other two models(BiLSTM-CRF, MT-BiLSTM-CRF), we identify that our models with CCL have a similar F1 score on non-shared slots. However, with CCL, both MT-BiLSTM-CRF-CCL and MT-BiLSTM-CCL achieves a significant improvement of F1 score on non-shared slots. This strongly demonstrates that CCL can effectively utilize the information of shared slots from multiple datasets.

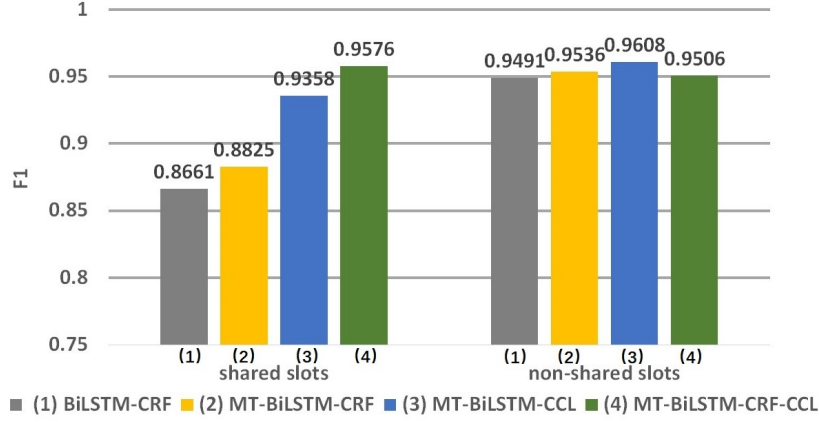


Fig. 2: F1 scores for shared slots and non-shared slots on the E-commerce camera dataset

## 5 Conclusion

In this paper, we focus on the phenomenon of shared slots between multiple slot filling tasks. In response to this phenomenon, we have proposed a deep multi-task architecture with CCL to capture the information of shared slots. To verify the validity of our approach, we build datasets in three domains. The experimental results show that our model can improve the performance of different slot filling tasks with shared slots. In addition, the proposed method is directly effective and can be easily applied to a similar multi-task model. In the future, we will try to use the CCL to solve other similar problems like text classification tasks with same labels.

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